

From Quantum Structures to GMV-algebras and Back

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It is well-known that every orthomodular lattice can be covered by blocks that are Boolean algebras, also every lattice ordered effect algebras can be covered by blocks that are MV-algebras. Hence the importance of MV-algebras for quantum structures is fundamental.

In the present talk we show that similar role can be founded also for pseudo effect algebras. Therefore, we study GMV-algebras, that are intervals in unital ℓ -groups with strong unit. Using this basic representation theorem we show many important classes of GMV-algebras.

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