THE BLOCK STRUCTURE OF COMPLETE LATTICE ORDERED EFFECT ALGEBRAS

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ABSTRACT. In [3], Riečanová proved that every lattice ordered effect algebra is a union of (essentially) MV-algebras. This result is a generalization of the well-known fact that every orthomodular lattice is a union of Boolean algebras. Later, Riečanová and Jenča proved in [2] that the set of all sharp elements of a lattice ordered effect algebra forms an orthomodular lattice. Both papers show that the class of lattice ordered effect algebras generalizes the class of orthomodular lattices in a very natural way.

We prove that every for every complete lattice ordered effect algebra E there exists an orthomodular lattice O(E) and a surjective full morphism $\phi_E : O(E) \to E$. ϕ_E preserves blocks in both directions: the (pre)image of a block is always a block. Moreover, there is a 0, 1-lattice embedding $\phi_E^* : E \to O(E)$ such that $\phi_E^* \circ \phi_E = id_E$.

Thus, for every complete lattice ordered effect algebra there is an orthomodular lattice with the same block structure. For the finite case, this result was proved in [1].

References

- G. Jenča. Finite homogeneous and lattice ordered effect algebras. Discrete Mathematics, 272:197–214, 2003.
- [2] G. Jenča and Z. Riečanová. On sharp elements in lattice ordered effect algebras. BUSEFAL, 80:24–29, 1999.
- [3] Z. Riečanová. A generalization of blocks for lattice effect algebras. Int. J. Theor. Phys., 39:855-865, 2000.

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