

V nasledujúcich úlohách určte dĺžku kriviek:

$$y = \frac{1}{3}(x^2 + 2)^{\frac{3}{2}}, x \in \langle 0, 3 \rangle$$

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$$y = \frac{x^2}{4}, x \in \langle 0, 2\sqrt{2} \rangle$$

$$\ln(\sqrt{3} + \sqrt{2}) + \sqrt{6}$$

$$y = \ln \sin x, x \in \langle \frac{\pi}{3}, \frac{\pi}{2} \rangle$$

$$\ln \sqrt{3}$$

$$y = \frac{2}{3}x\sqrt{x}, x \in \langle 0, 1 \rangle$$

$$\frac{2}{3}(2\sqrt{2} - 1)$$

$$y = \frac{x^2}{4} - \frac{1}{2} \ln x, x \in \langle 1, 2 \rangle$$

$$\frac{3}{4} + \ln \sqrt{2}$$

$$y = \ln \frac{e^x + 1}{e^x - 1}, y \in \langle \ln 2, \ln 5 \rangle$$

$$\ln \frac{16}{5}$$

$$y = \ln \frac{e^x + 1}{e^x - 1}, y \in \langle a, b \rangle$$

$$(a - b) + \ln \frac{e^{2b} - 1}{e^{2a} - 1}$$

$$y = \cosh x, x \in \langle 0, 1 \rangle$$

$$\sinh 1 = \frac{1}{2}(e - \frac{1}{e})$$

$$y = \ln x, x \in \langle \sqrt{3}, \sqrt{8} \rangle$$

$$1 + \frac{1}{2} \ln \frac{3}{2}$$

$$y = \arcsin x + \sqrt{1 - x^2}, x \in \langle 0, 1 \rangle$$

$$2(2 - \sqrt{2})$$

$$y = 2\sqrt{x}, x \in \langle 1, 2 \rangle$$

$$\ln(\sqrt{2} - 1) + \ln(\sqrt{\frac{3}{2}} - 1) + \frac{1}{2} \ln 2 - \sqrt{2} + \sqrt{6}$$

$$x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}, a > 0$$

6a

$$y^2 = 4x^3, y > 0, x \in \langle 0, 2 \rangle$$

$$\frac{2}{27}(19\sqrt{19} - 1)$$

$$y = 2x - x^2, x \in \langle 0, 1 \rangle$$

$$\frac{\sqrt{5}}{2} + \frac{1}{4} \ln(\sqrt{5} + 2)$$

$$y = \frac{2+x^6}{8x^2}, x \in \langle 1, 2 \rangle$$

$\frac{33}{16}$